

Zadaci za vežbu (izvodi)

1. Izračunati:

$$\begin{array}{ll} a) \ (x^2 - 3x + 2)' = & \\ b) \ (x - \sin x + \frac{1}{x})' = & \\ c) \ (2x^5 - \frac{1}{4}x^4 - \frac{2}{x} + \frac{3}{x^3})' = & \\ d) \ (\sqrt{x} + \sqrt[3]{x} - 2\sqrt[3]{x^2})' = & \\ e) \ (\frac{1}{\sqrt{x}} - \frac{1}{\sqrt[3]{x}})' = & \end{array}$$

$$\begin{array}{ll} f) \ (\sin x - \cos x)' = & \\ g) \ (2\operatorname{tg} x - \ln x)' = & \\ h) \ (2x^3 - 3\operatorname{ctg} x)' = & \\ i) \ (2\ln x - \frac{1}{x})' = & \\ j) \ (3e^x + 2\sqrt{x})' = & \end{array}$$

2. Izračunati:

$$\begin{array}{ll} a) \ (x^2 e^x)' = & \\ b) \ (\ln x \sin x)' = & \\ c) \ ((\sqrt{x} - 1)\sin x)' = & \\ d) \ (\ln^2 x)' = & \\ e) \ (2\operatorname{tg} x(\sin x - \operatorname{ctg} x))' = & \end{array}$$

$$\begin{array}{ll} f) \ (x \sin x \ln x)' = & \\ g) \ ((\frac{x^3}{3} + x)\operatorname{arctg} x)' = & \\ h) \ (\operatorname{arcsin} x \operatorname{arccos} x)' = & \\ i) \ (\sqrt{x} \operatorname{arcsin} x)' = & \end{array}$$

3. Izračunati:

$$\begin{array}{ll} a) \ (\frac{x}{\sin x})' = & \\ b) \ (\frac{\sin x}{\cos x})' = & \\ c) \ (\frac{1}{\sqrt{x} + 1})' = & \\ d) \ (\frac{e^x}{x + x^2})' = & \\ e) \ (\frac{2 - \operatorname{arctg} x}{1 + \operatorname{arctg} x})' = & \end{array}$$

$$\begin{array}{ll} f) \ (\frac{x}{\ln x})' = & \\ g) \ (\frac{x \ln x}{\sin x})' = & \\ h) \ (\frac{1}{\ln x} - \frac{1}{e^x})' = & \\ i) \ (\frac{\operatorname{arcsin} x}{x} - \frac{\sin x}{\sqrt{x}})' = & \end{array}$$

4. Naći izvode sledećih funkcija:

$$\begin{array}{lll} a) \ f(x) = (x + 2)^2 & f) \ f(x) = \ln(x + 1) & k) \ f(x) = \operatorname{tg}(\sin x) \\ b) \ f(x) = \sin(2x - 1) & g) \ f(x) = \cos(2x) & l) \ f(x) = \sqrt{\cos x} \\ c) \ f(x) = e^{\sqrt{x}} & h) \ f(x) = \sqrt[3]{x^2 - 3} & m) \ f(x) = \ln(\ln x) \\ d) \ f(x) = \sin^5 x & i) \ f(x) = \operatorname{arctg} x^2 & n) \ f(x) = e^{\cos x} \\ e) \ f(x) = \sin x^5 & j) \ f(x) = e^{3x-1} & nj) \ f(x) = \sqrt{x^2 - 3x + 2} \end{array}$$

5. Naći izvode sledećih funkcija:

$$\begin{array}{lll} a) \ f(x) = (x^4 + 3x^2 + 3)^5 & f) \ f(x) = \frac{2x + 3}{\sqrt{4x^2 + 9}} & k) \ f(x) = \operatorname{arctg}(\frac{1 + x}{1 - x}) \\ b) \ f(t) = (t^2 + 1)^2 & g) \ f(x) = \sin 2x + \cos 5x & l) \ f(x) = \operatorname{arcsin} \sqrt{x} - e^{\sin x + \cos x} \\ c) \ f(s) = \sqrt[3]{5s^2 - s - 3} & h) \ f(x) = 3\sin^5 x + \operatorname{tg} \sqrt{x} & lj) \ f(x) = \ln(\frac{1 + x}{1 - x}) \\ d) \ f(x) = (3x - 1)^6 \sqrt{2x - 5} & i) \ f(x) = (\sin x + \cos x)^2 & m) \ f(x) = e^{x^2 + 3x + 1} \\ e) \ f(x) = \sqrt{\frac{x}{x + 1}} & j) \ f(x) = \sqrt{\operatorname{arctg} x} + \operatorname{tg} x & n) \ f(x) = \ln \sqrt{x^2 + 2} + \sqrt{\ln(x^2 + 2)} \end{array}$$

6. Naći izvode sledećih funkcija:

$$a) \quad f(x) = \frac{2x^2 - 3x + 1}{x^2 + 1} \quad f) \quad f(x) = 5 \operatorname{arctg}(2x + 7)e^{3x+1}$$

$$b) \quad f(x) = \frac{\sin x + e^x \tan x}{\ln x + 1} \quad g) \quad f(x) = 2\sqrt{\cos x} + \ln(x^2 + 1)$$

$$c) \quad f(x) = \frac{\sin x - \cos x}{\sin x + \cos x} \quad h) \quad f(x) = \frac{\sin x + \tan x}{x^3 + e^x + 3x}$$

$$d) \quad f(x) = \frac{\sin^2 x + 2x \cos x}{e^x + 1} \quad i) \quad f(x) = \sin(\sqrt{3}x) - \sqrt{3} \sin x$$